

3.2.1 Backtracking Example

```
member(X, [X|_]).  
member(X, [_|L]) :-  
    member(X, L).
```

Initial query: `member(Z, [a,b]), member(Z, [b,c])`

Both clauses match first goal; choose first and **push a choicepoint**

$Z = X = a$

New query: `member(a, [b,c])`

Clause 1 does not match; clause 2 matches with

$X1 = a, \quad L1 = [c]$

[-] Backtracking Example (2)

New query: `member(a, [c])`

Clause 1 does not match; clause 2 matches with

$X2 = a, \quad L2 = []$

New query: `member(a, [])`

Neither clause matches: failure

[-] Backtracking Example (3)

We are not done; we pop the choicepoint off the stack

This returns us to state at time the choicepoint was pushed, but now we go on to the next clause

New query: $\text{member}(Z, [a,b]), \text{member}(Z, [b,c])$

Now choose second clause, with

$Z = X, \quad L = [b]$

New query: $\text{member}(Z, [b]), \text{member}(Z, [b,c])$

Both clauses match first goal; choose first and **push a choicepoint**

$Z = X = b$

[-] Backtracking Example (4)

New query: `member(b, [b,c])`

Both clauses match first goal; choose first and **push a choicepoint**

$X2 = b$

New query is empty: success, leaving

$Z = b$

Prolog prints this result; if we hit ; asking for more solutions, this forces an artificial failure, causing Prolog to backtrack, looking for more solutions

Backtracking Example (5)

New query: `member(b, [b,c])`

Clause 2 matches with $X2 = b$, $L2 = [c]$

New query: `member(b, [c])`

Clause 2 matches with $X3 = b$, $L3 = []$

New query: `member(b, [])`

Neither clause matches: pop last choicepoint

New query: `member(Z, [b]), member(Z, [b,c])`

Second clause matches, leaving

$X3 = Z$, $L3 = []$

New query: `member(Z, []), member(Z, [b,c])`

Neither clause matches: final failure

3.2.2 Example: Search Tree

