

Show all work. 5 points each.

1. Find the Laurent series for $f(z) = \frac{e^{z^2} - 1}{z^4}$. Find the order of the pole at zero as well as the residue.

2. Use $\text{Res}(f(z), z_k) = \frac{1}{(n-1)!} \lim_{z \rightarrow z_k} \frac{d^{n-1}}{dz} (z - z_k)^n f(z)$ to find the residues for all the poles of $f(z) = \frac{1}{(z^2 + 1)^3}$.