

Show all work. 5 points each.

1. Find a potential function f so that $\mathbf{F} = \langle xy^2, x^2y \rangle = \nabla f$ and use it to evaluate $\int_C \mathbf{F} \cdot d\mathbf{r}$ where $C: \mathbf{r}(t) = \langle t + \sin(\frac{\pi t}{2}), t + \cos(\frac{\pi t}{2}) \rangle$, $0 \leq t \leq 1$.

2. Use Greens theorem to evaluate $\oint_C xy \, dx + x^2y^3 \, dy$ where C is the triangle with vertices $(0, 0)$, $(1, 0)$ and $(1, 2)$