

How many Molecules of SiO₂ are in my Quartz Sphere?

Quartz Sphere:

$$m = 346.3 \text{ g}$$

$$D = 6.30 \text{ cm} \Rightarrow R = 3.15 \text{ cm}$$

$$\Rightarrow V = [(4/3)\pi R^3] = 130.9 \text{ cm}^3$$

$$\text{Density} = \rho = m/V = m/[(4/3)\pi R^3] = 346.3\text{g}/130.9 \text{ cm}^3 = 2.645 \text{ g/cm}^3 = 2.65 \text{ g/cm}^3$$

$$\text{Given Density and Volume} \Rightarrow \text{Mass: } m = \rho V = 346.3 \text{ g}$$

What is the mass of one Molecule of SiO₂ (Quartz)?

$Z \equiv$ Atomic Number of an Element = # of Protons in Nucleus = # of electrons in atom
 $N \equiv$ = # of Neutrons in Nucleus \approx usually $\approx Z$

A = Atomic Weight of an Atom of an Element $\approx Z + N$
is given in units called: amu = Atomic Mass Units

$$1 \text{ amu} \equiv (1/12) \{ \text{Mass of Carbon 12 (with } Z + N = 6 + 6 = 12) \}$$
$$= 1.66053886 \times 10^{-24} \text{ grams}$$

$$1 \text{ amu} \approx \text{mass of the proton} \approx \text{mass of the Neutron} \approx \text{mass of a Nucleon}$$
$$\approx \text{mass of a Hydrogen Atom (since electrons have mass} \approx \text{amu}/1823)$$
$$\approx [1/(6.02 \times 10^{23})] \text{ grams} = [1/(\text{Avogadro's Number})] \text{ grams}$$

$$\text{where: } 1 \text{ mole} \equiv \text{Avogadro's Number} = 6.02 \times 10^{23}$$

$$\Rightarrow (6.02 \times 10^{23}) \text{ amu} = 1 \text{ gram}$$

$$\text{or: Mass of a mole of Nucleons} = 1 \text{ gram}$$

MW = Molecular Weight of SiO₂:

$$\approx [A_{\text{Si}} = Z + N = 2 \cdot Z_{\text{Si}} = 2 \cdot 14 = 28] + 2 \cdot [A_{\text{O}} = Z + N = 2 \cdot Z_{\text{O}} = 2 \cdot 8 = 16]$$

$$= 60 \text{ amu} = \# \text{ of Protons} + \# \text{ of Neutrons}$$

$$= 28.0855 + 2 \cdot 15.9994 = 60.0843 \text{ amu (from Tables or a good Periodic Table)}$$

$$\text{Mass in grams of SiO}_2 = 60.0843 \text{ amu} [1.66053886 \times 10^{-24} \text{ g/amu}] = 9.977 \times 10^{-23} \text{ g}$$
$$[1.661 \times 10^{-24} \text{ g/amu}] =$$
$$[1/(6.02 \times 10^{23}) \text{ g/amu}] =$$
$$[1\text{g} / (6.02 \times 10^{23} \text{ amu})] =$$

$$\text{Mass in grams of SiO}_2 = 60.0843 \text{ amu} [1\text{g} / (\text{mole amu})] \text{ since mole} = 6.02 \times 10^{23}$$
$$= 60 \text{ grams/mole}$$

$$\Rightarrow \text{Mass of 1 mole in grams of SiO}_2 = 60 \text{ grams} = \text{MW in grams}$$

In General: MW in grams = Mass of a Mole of Molecules

$$n = \# \text{ of Molecules in Quartz Sphere} = [\text{mass of } n \text{ Molecules}] / [\text{mass of 1 Molecule}]$$
$$= [\text{mass of our Sample}] / [\text{mass of 1 Molecule}]$$
$$= [346.3 \text{ g}] / [9.977 \times 10^{-23} \text{ g}]$$
$$= 3.471 \times 10^{24} \text{ Molecules}$$
$$= 3.47 \times 10^{24} \text{ Molecules} [1 \text{ mole} / 6.02 \times 10^{23} \text{ Molecules}]$$
$$= 5.77 \text{ moles of molecules}$$

or equivalently:

$$\# \text{ of moles of Molecules in Quartz Sphere} = [\text{mass of our Sample}] / [\text{mass of 1 mole}]$$
$$= [346.3 \text{ g}] / [60 \text{ g}]$$
$$= 5.77 \text{ moles}$$

Remember:

$$1 \text{ amu} \approx \text{mass of the proton} \approx \text{mass of the Neutron} \approx \text{mass of a Nucleon}$$
$$\approx \text{mass of a Hydrogen Atom (since electrons have mass} \approx \text{amu}/1823)$$
$$\approx [1/(6.02 \times 10^{23})] \text{ grams} = [1/(\text{Avogadro's Number})] \text{ grams}$$