

**Show all necessary steps in each problem. Full credit is based on work shown!**

1. Use fundamental identities to establish the following identities.

5pts [Hint: substitute & simplify.]

3pts [Hint: substitute & simplify.]

a.  $\frac{1 - \sin \theta}{\cos \theta} + \frac{\cos \theta}{1 - \sin \theta} = 2 \sec \theta$

b.  $(\tan \theta \cot \theta) - \sin^2 \theta = \cos^2 \theta$

4pts

2. Use the sum and difference identities to write the expression as the sine, cosine or tangent of a single angle, then give the **exact value** of the function.

a.  $\sin 115^\circ \cos 35^\circ + \cos 115^\circ \sin 35^\circ$

b.  $\frac{\tan 40^\circ - \tan 70^\circ}{1 + \tan 40^\circ \tan 70^\circ}$

8pts

3. Given that  $\sin \alpha = \frac{-12}{13}$ , where  $\pi < \alpha < \frac{3\pi}{2}$ ; and  $\cos \beta = \frac{\sqrt{6}}{5}$ , where  $\frac{3\pi}{2} < \beta < 2\pi$

Sketch triangles to find the exact value of:

a.  $\cos \alpha$

b.  $\sin \beta$

Then calculate:

c.  $\cos(\alpha + \beta)$