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Show all work. 5 points each.

1. Find the inverse of the matrix  $\begin{bmatrix} 8 & 6 \\ 5 & 4 \end{bmatrix}$  and **USE IT** to solve the system of equations

$$\begin{aligned} 8x_1 + 6x_2 &= 2 \\ 5x_1 + 4x_2 &= -1. \end{aligned}$$

2. True/False don't need to justify. **All matrices are  $n \times n$  for this exercise.**

- a) If the equation  $A\mathbf{x} = \mathbf{b}$  has more than one solution for at least one  $\mathbf{b} \in \mathbb{R}^n$ , then the matrix  $A$  is invertible.
- b) If  $A^T$  is not invertible, then  $A$  is not invertible.
- c) If matrices  $E$  and  $F$  have the property that  $EF = I$ , then  $EF = FE$ .
- d) If  $K$  is an invertible matrix then,  $AK = KA$  for all other  $n \times n$  matrices  $A$ .
- e) If  $A$  and  $B$  are invertible  $AB$  is invertible and the inverse is  $A^{-1}B^{-1}$ .