

MAT 346 Review II

I. Mathematics Topics

a. Algebra

- i. Descartes' Factor Theorem
- ii. Fundamental Theorem of Algebra

b. Numbers

- i. Primes, Fermat primes
- ii. Formulae for π
- iii. Factorials
- iv. Combinatorial (Pascal)
- v. Riemann zeta function
 1. Connection to primes
 2. General properties
- vi. Euler's Constant
- vii. AGM (Arithmetic-Geometric Mean)
- viii. Germain Prime
- ix. Fermat's Little Theorem
- x. Euler's ϕ -function

c. Projective Geometry

- i. Pappus' Theorem
- ii. Perspective
- iii. Vanishing points
- iv. Horizon
- v. Cross-ratio
- vi. Homogeneous coordinates
- vii. Point(s) at infinity
- viii. Projective Lines
- ix. Projective sphere
- x. How do lines, circles, conics project?

d. Non-Euclidean Geometry

- i. Parallel postulate
- ii. Three types of geometry
- iii. Curvature and types
- iv. Sum of angles
- v. Sphere
- vi. Pseudosphere
- vii. Hyperbolic plane
- viii. Beltrami-Poincare model
- ix. Beltrami-Klein model
- x. Poincare disk
- xi. Geodesics
- xii. Hyperboloids
- xiii. Riemannian geometry
- xiv. Hyperbolic geometry

e. Equations

- i. Cubic

- ii. Biquadratic

- iii. Quintic

f. Infinite Series

- i. Geometric
- ii. Logarithm
- iii. Exponential
- iv. Sine, Cosine
- v. Binomial
- vi. Harmonic
- vii. Power series
- viii. Telescoping
- ix. Inversion of series
- x. Basel Problem
- xi. Euler's Trick

g. Calculus

- i. Tangents
- ii. Infinitesimals
- iii. Indivisibles
- iv. Method of Exhaustion
- v. How did Wallis integrate powers?
- vi. Arclength
- vii. Rectification
- viii. Fundamental Theorem of Calculus

h. Curves

- i. Conics
- ii. Archimedean spiral
- iii. Conchoid, cissoids
- iv. Cycloid
- v. Ellipse
- vi. Lemniscate

i. Elliptic Functions

j. Complex Numbers

- i. Argand diagram
- ii. Euler's Formula
- iii. De Moivre's Formula
- iv. Roots of unity
- v. Stereographic Projection
- vi. Conformal map
- vii. Riemann surfaces
- viii. Relation to torus

k. Tiling

- i. Polygons
- ii. Circle Limits
- iii. Schläfli symbol
- iv. Nonperiodic

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- v. Penrose tiling – kites, darts, thin and thick rhoms
- vi. Einstein tiles – hat, spectre
- vii. Polyominoes
- viii. pentominoes
- I. Group Theory
 - i. Properties of groups
 - ii. Permutation group
 - iii. Permutations
- II. Hardy, Littlewood, Ramanujan
 - a. Taxicab numbers
 - b. 1729
- III. People
 - a. Eudoxus
 - b. Archimedes
 - c. Pappus of Alexandria
 - d. Proclus
 - e. Saccheri
 - f. Madhava
 - g. Brunelleschi
 - h. Cardano
 - i. Bombelli
 - j. Harriot
 - k. Desargues
 - l. Descartes
 - m. Mersenne
 - n. Cavalieri
 - o. Fermat
 - p. Argand
 - q. Wessel
 - r. Roberval
 - s. Torricelli
 - t. Wallis
 - u. Barrow
 - v. Gregory
 - w. Taylor
 - x. Cotes
 - y. Mercator
 - z. Newton
 - aa. Leibniz
 - bb. Bernoulli (Johann, Jacob, Daniel, Nicholas, ...)
 - cc. Euler
 - dd. Laplace
 - ee. d'Alembert
 - ff. de Moivre
 - gg. Gauss
 - hh. Cauchy
 - ii. Galois
 - jj. Vandermonde
 - kk. Oresme
 - ll. Abel
 - mm. Jacobi
 - nn. Fagnano
 - oo. Mobius
 - pp. Legendre
 - qq. Laguerre
 - rr. Bolyai
 - ss. Lobachevsky
 - tt. Beltrami
 - uu. Klein
 - vv. Poincare
 - ww. Poisson
 - xx. Liouville
 - yy. Fourier
 - zz. Riemann
 - aaa. Weierstrass
 - bbb. Germain
 - ccc. Somerville
 - ddd. Lovelace
 - eee. Nightingale
 - fff. Kovalevskaya
 - ggg. Bassi
 - hhh. Babbage
 - iii. Penrose
 - jjj. Escher
 - kkk. Durer
- IV. Books
 - a. Principia (Philosophiae Naturalis Principia Mathematica)
 - b. Arithmetica Infinitorum
 - c. Disquisitiones Arithmeticae