

MAT 261 Exam III

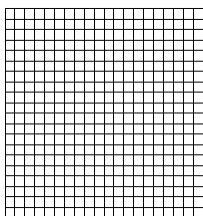
Name _____

Problem	Score
1 (20 pts)	
2 (30 pts)	
3 (25 pts)	
4 (25 pts)	
Total (100 pts)	

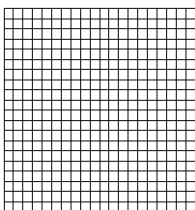
1. Functions (20 pts)

a. State and sketch the domain of the function

$$f(x, y) = \sqrt{x+y}.$$



b. Sketch and label at least 5 level curves for the function $f(x, y) = 1 - x^2$.



c. Sketch the function in part b.

d. Show that $\lim_{(x,y) \rightarrow (0,0)} \frac{x^2y}{x^3+y^3}$ does not exist.

2. Partial Derivatives (30 pts)

a. Let $g(x, y) = x^5 + 3x^3y^2 + 3xy^4$.

i) Find $\frac{\partial g}{\partial x}$.

ii) Find $\frac{\partial^3 g}{\partial x^2 \partial y}$.

b) For $x^2 + y^2 + z^2 = xz$ determine $\frac{\partial z}{\partial x}$.

c) Find $\frac{\partial z}{\partial t}$ for $z = x^2 + xy + y^2$, $x = s + 2t$, $y = st$.

d) Draw a tree diagram for the chain rule for $u = u(x, y, z)$, $x = x(s, t)$, $y = y(s, t)$, $z = z(s, t)$. Label one branch involving derivatives of u with respect to t .

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3. Miscellaneous (25 pts) Let $f(x, y) = xe^y$.a. Find the gradient of $f(x, y)$.b. Find the directional derivative of $f(x, y)$ at $(2, 0)$ in the direction $\langle 2, 1 \rangle$.c. What is the maximum rate of change of $f(x, y)$ at $(2, 0)$?d. Linearize the given function at $(2, 0)$.e. Express df in terms of dx and dy .**4. Maxima and Minima (25 pts)**

a. State the Second Derivative Test for classifying critical points.

b. Determine the nature of the critical points for the function $f(x, y) = x^3 + y^2 - 12x + 2y$.c. Use Lagrange multipliers to find the maximum and minimum values of $f(x, y) = x^2y$ subject to the constraint $x^2 + y^2 = 5$.