

## MAT 162 Review – Chapter 11

### 1. Sequences [Exam A](#)

- Convergence and divergence
- Special limits

c.  $\lim_{x \rightarrow \infty} \sqrt[n]{n} = 1$ ,  $\lim_{x \rightarrow \infty} \frac{\ln n}{n} = 0$ ,  $\lim_{x \rightarrow \infty} \sqrt[n]{x} = 1$ ,  $\lim_{x \rightarrow \infty} \left(1 + \frac{x}{n}\right)^n = e^x$ ,  $\lim_{x \rightarrow \infty} x^n = 0$ ,  $|x| < 1$ ,

- Recursive definitions

### 2. Infinite Series [Exam A](#)

- $n$ th Partial Sum
- Convergence vs Divergence

c. Geometric Series:  $\sum_{n=0}^{\infty} ar^n = a + ar + ar^2 + \dots$  Converges:  $S = \frac{a}{1-r}$ ,  $|r| < 1$ ; Diverges:  $|r| \geq 1$

- Harmonic series, alternating harmonic series,  $p$ -series
- $n$ th term divergence test
- Convergence Tests – Comparison, Limit Comparison, Integral Test, Ratio Test, Root Test
- Alternating Series and Alternating Series (Leibniz) Test
- Conditional vs Absolute Convergence
- Remainder estimates

### 3. Power Series $\sum_{n=0}^{\infty} c_n (x-a)^n$ [Exam B](#)

- Radius and Interval of Convergence ([Ratio & Root tests](#))
- Functions as Power Series – use of geometric series to develop new series, differentiation and integration of power series. ([Know geometric series](#))

### 4. Taylor-Maclaurin Series [Exam B](#)

a.  $f(x) = f(a) + f'(a)(x-a) + \frac{f''(a)}{2!}(x-a)^2 + \frac{f'''(a)}{3!}(x-a)^3 + \dots + \frac{f^{(n)}(a)}{n!}(x-a)^n + \dots$

- Interval of Convergence  $|x-a| < R$

- Special Maclaurin Series

i.  $e^x = 1 + x + \frac{x^2}{2!} + \frac{x^3}{3!} + \dots + \frac{x^n}{n!} + \dots$  for  $(-\infty, \infty)$

ii.  $\cos x = 1 - \frac{x^2}{2} + \frac{x^4}{4!} + \dots$

iii.  $\sin x = x - \frac{x^3}{3!} + \frac{x^5}{5!} + \dots$

iv.  $\frac{1}{1-x} = 1 + x + x^2 + x^3 + \dots + x^n + \dots$

v.  $\ln(1+x) = x - \frac{x^2}{2} + \frac{x^3}{3} - \frac{x^4}{4} + \dots + \frac{(-1)^n x^{n+1}}{n+1} + \dots$

vi.  $\tan^{-1} x = x - \frac{x^3}{3} + \frac{x^5}{5} - \frac{x^7}{7} + \dots$

$$(1+x)^k = 1 + kx + \frac{k(k-1)}{2!}x^2 + \frac{k(k-1)(k-2)}{3!}x^3 + \dots$$

- Binomial Series:

$$= \sum_{n=0}^{\infty} \binom{k}{n} x^n$$