

1. A tank holds 1000 gallons of water, which drains from the bottom of the tank in half an hour. The values in the table show the volume  $V$  of water remaining in the tank (in gallons) after  $t$  minutes.

$t$ (min)	5	10	15	20	25	30
$V$ (gal)	694	444	250	111	28	0

- (a) If  $P$  is the point  $(15, 250)$  on the graph of  $V$ , find the slopes of the secant lines  $PQ$  when  $Q$  is the point on the graph with  $t = 5, 10, 20, 25,$  and  $30$ .
- (b) Estimate the slope of the tangent line at  $P$  by averaging the slopes of two secant lines.
- (c) Use a graph of the function to estimate the slope of the tangent line at  $P$ . (This slope represents the rate at which the water is flowing from the tank after 15 minutes.)

3. The point  $P(2, -1)$  lies on the curve  $y = 1/(1 - x)$ .

- (a) If  $Q$  is the point  $(x, 1/(1 - x))$ , use your calculator to find the slope of the secant line  $PQ$  (correct to six decimal places) for the following values of  $x$ :

(i) 1.5      (ii) 1.9      (iii) 1.99      (iv) 1.999  
 (v) 2.5      (vi) 2.1      (vii) 2.01      (viii) 2.001

- (b) Using the results of part (a), guess the value of the slope of the tangent line to the curve at  $P(2, -1)$ .
- (c) Using the slope from part (b), find an equation of the tangent line to the curve at  $P(2, -1)$ .

5. If a ball is thrown into the air with a velocity of 40 ft/s, its height in feet  $t$  seconds later is given by  $y = 40t - 16t^2$ .

- (a) Find the average velocity for the time period beginning when  $t = 2$  and lasting

(i) 0.5 second      (ii) 0.1 second  
 (iii) 0.05 second      (iv) 0.01 second

- (b) Estimate the instantaneous velocity when  $t = 2$ .